



# Assignment

## Value of Function

### Basic Level

If  $f(x) = \frac{1-x}{1+x}$ , then  $f[f(\cos 2\theta)]$  equal to [MP PET 1994, 2001]

- (a)  $\tan 2\theta$                       (b)  $\sec 2\theta$                       (c)  $\cos 2\theta$                       (d)  $\cot 2\theta$

If  $f(x) = \frac{\cos^2 x + \sin^4 x}{\sin^2 x + \cos^4 x}$  for  $x \in R$ , then  $f(2002) =$  [EAMCET 2002]

- (a) 1                                  (b) 2                                  (c) 3                                  (d) 4

If  $\phi(x) = a^x$ , then  $\{\phi(p)\}^3$  is equal to [MP PET 1999]

- (a)  $\phi(3p)$                       (b)  $3\phi(p)$                       (c)  $6\phi(p)$                       (d)  $2\phi(p)$

If  $f(x) = \cos(\log x)$ , then  $f(x)f(y) - \frac{1}{2}[f(\frac{x}{y}) + f(xy)] =$  [IIT 1983; Rajasthan PET 1995; MP PET 1995; KCET 1999; UPSEAT 2001]

- (a)  $\frac{1}{2}$                               (b) 2                              (c) 0                              (d) 1

If  $f(\theta) = \tan \theta$ , then  $\frac{f(\theta) - f(\phi)}{1 + f(\theta)f(\phi)}$  is equal to [Rajasthan PET 1996]

- (a)  $f(\theta - \phi)$                       (b)  $f(\phi - \theta)$                       (c)  $f(\theta + \phi)$                       (d) None of these

If  $f(x) = 2x\sqrt{1-x^2}$ , then  $f\left(\sin \frac{x}{2}\right)$  equals [Rajasthan PET 1989]

- (a)  $\sin 2x$                       (b)  $\sin x$                       (c)  $2 \sin x$                       (d)  $2 \sin \frac{x}{2}$

If  $f(x) = \frac{x}{x-1}$ , then  $\frac{f(a)}{f(a+1)}$  is equal to [MP PET 1996]

- (a)  $f(-a)$                       (b)  $f\left(\frac{1}{a}\right)$                       (c)  $f(a^2)$                       (d)  $f\left(\frac{-a}{a-1}\right)$

If  $f(x) = \begin{cases} 2x-3 & , x \geq 2 \\ x & , x < 2 \end{cases}$ , then  $f(1)$  is equal to [Karnataka CET 1989]

- (a)  $2f(2)$                       (b)  $f(2)$                       (c)  $-f(2)$                       (d)  $\frac{1}{2}f(2)$

If  $f(x) = x^2 - x^{-2}$ , then  $f\left(\frac{1}{x}\right)$  is equal to [SCRA 1999]

- (a)  $f(x)$                       (b)  $-f(x)$                       (c)  $\frac{1}{f(x)}$                       (d)  $[f(x)]^2$



If  $f(x) = 4x^3 + 3x^2 + 3x + 4$ , then  $x^3 f\left(\frac{1}{x}\right)$  is

[SCRA 1996]

- (a)  $f(-x)$  (b)  $\frac{1}{f(x)}$  (c)  $\left[f\left(\frac{1}{x}\right)\right]^2$  (d)  $f(x)$

The equivalent function of  $\log x^2$  is

[MP PET 1997]

- (a)  $2 \log x$  (b)  $2 \log |x|$  (c)  $|\log x^2|$  (d)  $(\log x)^2$

### Advance

If  $f(x) = \cos[\pi]x + \cos[\pi x]$ , where  $[y]$  is the greatest integer function of  $y$  then  $f\left(\frac{\pi}{2}\right)$  is equal to

- (a)  $\cos 3$  (b) 0 (c)  $\cos 4$  (d) None of these

Let  $f(x) = \begin{cases} 1+|x| & , x < -1 \\ [x] & , x \geq -1 \end{cases}$ , where  $[.]$  denotes the greatest integer function. Then  $f\{f(-2.3)\}$  is equal to

- (a) 4 (b) 2 (c) -3 (d) 3

If  $f(x_1) + f(x_2) = f\left(\frac{x_1 + x_2}{1 + x_1 x_2}\right)$ ,  $x_1, x_2 \in (-1, 1)$ , then  $f(x)$  is equal to

[Roorkee 1998]

- (a)  $\log\left(\frac{1-x}{1+x}\right)$  (b)  $\tan^{-1}\left(\frac{1-x}{1+x}\right)$  (c)  $\log\left(\frac{2x}{1-x^2}\right)$  (d)  $\tan^{-1}\left(\frac{1+x}{1-x}\right)$

If  $f(x) = \frac{|x|}{x}$ ,  $x \neq 0$ , then the value of function

[BIT Mesra 1999]

- (a) 1 (b) 0 (c) -1 (d) Does not exist

If a function  $g(x)$  is defined in  $[-1, 1]$  and two vertices of an equilateral triangle are  $(0, 0)$  and  $(x, g(x))$  and its area is  $\frac{\sqrt{3}}{4}$ , then  $g(x)$  equals [IIT 1989]

- (a)  $\sqrt{1+x^2}$  (b)  $-\sqrt{1+x^2}$  (c)  $\sqrt{1-x^2}$  (d) None of these

If  $f(x) = \frac{2^x + 2^{-x}}{2}$ , then  $f(x+y) \cdot f(x-y)$  is equal to

[Rajasthan PET 1998]

- (a)  $\frac{1}{2}[f(x+y) + f(x-y)]$  (b)  $\frac{1}{2}[f(2x) + f(2y)]$  (c)  $\frac{1}{2}[f(x+y) \cdot f(x-y)]$  (d) None of these

$f(1) = 1$  and  $f(n+1) = 2f(n) + 1$  if  $n \geq 1$ , then  $f(n)$  is

[Karnataka CET 1994; IIT 1995]

- (a)  $2^{n+1}$  (b)  $2^n$  (c)  $2^n - 1$  (d)  $2^{n-1} - 1$

If  $2f(x) - 3f(1/x) = x^2$ ,  $x \neq 0$ , then  $f(2)$  is equal to

[IIT 1991]

- (a)  $5/2$  (b)  $-7/4$  (c) -1 (d) None of these

If  $f(x) = x - 1$ , then correct statement is

[IIT 1983]

- (a)  $f(x^2) = [f(x)]^2$  (b)  $f(|x|) = f(x)$  (c)  $f(x+y) = f(x) + f(y)$  (d) None of these

## Domain of Function

### Basic Level

The domain of the function  $f(x) = \sqrt{\log_{0.5} x}$  is

[Roorkee 1990]

- (a)  $(0, 1]$  (b)  $(0, \infty)$  (c)  $(0.5, \infty)$  (d)  $[1, \infty)$

The domain of definition of the real function  $f(x) = \sqrt{\log_{12} x^2}$  of the real variable  $x$  is

- (a)  $x > 0$  (b)  $|x| \geq 1$  (c)  $|x| \geq 4$  (d)  $x \geq 4$



The natural domain of the real valued function defined by  $f(x) = \sqrt{x^2 - 1} + \sqrt{x^2 + 1}$  [SCRA 1996]

- (a)  $1 < x < \infty$  (b)  $-\infty < x < \infty$  (c)  $-\infty < x < -1$  (d)  $(-\infty, \infty) - (-1, 1)$

The domain of the function  $y = \sqrt{\frac{1}{x} - 1}$  is, [AMU 2000]

- (a)  $x \leq 1$  (b)  $0 \leq x \leq 1$  (c)  $0 \leq x < 1$  (d)  $0 < x \leq 1$

Domain of  $f(x) = \log |\log x|$  is [Pb. CET 1998; DCE 2002]

- (a)  $(0, \infty)$  (b)  $(1, \infty)$  (c)  $(0, 1) \cup (1, \infty)$  (d)  $(-\infty, 1)$

Domain of function  $f(x) = \left[ \log_{10} \left( \frac{5x - x^2}{4} \right) \right]^{1/2}$  is [UPSEAT 2001]

- (a)  $-\infty < x < \infty$  (b)  $1 \leq x \leq 4$  (c)  $4 \leq x \leq 16$  (d)  $-1 \leq x \leq 1$

Domain of the function  $\sin^{-1} \left[ \log_2 \left( \frac{x^2}{2} \right) \right]$  is [MP PET 1998]

- (a)  $[1, 2]$  (b)  $[-1, 2]$  (c)  $[-2, 2] - (-1, 1)$  (d)  $[-2, 2] - \{ \}$

The domain of the function  $f(x) = \frac{\sqrt{4 - x^2}}{\sin^{-1}(2 - x)}$  is

- (a)  $[0, 2]$  (b)  $[0, 2)$  (c)  $[1, 2)$  (d)  $[1, 2]$

The domain of the function  $f(x) = \log(\sqrt{x - 4} + \sqrt{6 - x})$  is [Rajasthan PET 2001]

- (a)  $[4, \infty)$  (b)  $(-\infty, 6]$  (c)  $[4, 6]$  (d) None of these

### Advance

The largest set of real values of  $x$  for which  $f(x) = \sqrt{(x+2)(5-x)} - \frac{1}{\sqrt{x^2 - 4}}$  is a real function

- (a)  $[1, 2] \cup (2, 5]$  (b)  $(2, 5]$  (c)  $[3, 4]$  (d) None of these

The domain of the function  $f(x) = \frac{1}{\log_{10}(1-x)} + \sqrt{x+2}$  is [DCE 2000]

- (a)  $] -3, -2.5[ \cup ] -2.5, -2[$  (b)  $[-2, 0[ \cup ] 0, 1[$   
 (c)  $] 0, 1[$  (d) None of these

The domain of the function  $f(x) = \log_e(x - [x])$ , where  $[.]$  denotes the greatest integer function, is

- (a)  $R$  (b)  $R - Z$  (c)  $(0, +\infty)$  (d) None of these

The domain of the function  $f(x) = \frac{\sin^{-1}(3-x)}{\ln(|x| - 2)}$  is [Orissa JEE 2002]

- (a)  $[2, 4]$  (b)  $(2, 3) \cup (3, 4]$  (c)  $[2, \infty)$  (d)  $(-\infty, -3) \cup [2, \infty)$

Domain of the function  $f(x) = \sin^{-1}(1 + 3x + 2x^2)$  is [Roorkee 2000]

- (a)  $(-\infty, \infty)$  (b)  $(-1, 1)$  (c)  $\left[ \frac{-3}{2}, 0 \right]$  (d)  $\left( -\infty, \frac{-1}{2} \right) \cup (2, \infty)$

Domain of the function  $\sin \ln \left( \frac{\sqrt{4-x^2}}{1-x} \right)$  [IIT 1985; Rajasthan PET 2003]

- (a)  $[-2, 1]$  (b)  $(-2, 1)$  (c)  $[-2, 1)$  (d)  $(-2, 1]$

Domain of the function  $f(x) = \sqrt{\log_{0.5}(3x-8) - \log_{0.5}(x^2+4)}$  is [AMU 1999]

- (a)  $\left(\frac{8}{3}, \infty\right)$                       (b)  $\left(-\infty, \frac{8}{3}\right)$                       (c)  $(-\infty, \infty)$                       (d)  $(0, \infty)$

The domain of  $f(x) = \frac{1}{\sqrt{|\cos x| + \cos x}}$  is

- (a)  $[-2n\pi, 2n\pi]$                       (b)  $(2n\pi, 2n+1\pi)$                       (c)  $\left(\frac{(4n+1)\pi}{2}, \frac{(4n+3)\pi}{2}\right)$                       (d)  $\left(\frac{(4n-1)\pi}{2}, \frac{(4n+1)\pi}{2}\right)$

The domain of  $f(x) = \sin^{-1}\left(\frac{1+x^2}{2x}\right) + \sqrt{1-x^2}$  is

- (a)  $\{1\}$                       (b)  $(-1, 1)$                       (c)  $\{1, -1\}$                       (d) None of these

The domain of the function  $f(x) = \sqrt{\log\left(\frac{1}{|\sin x|}\right)}$  is

[Rajasthan PET 2001]

- (a)  $R - \{-\pi, \pi\}$                       (b)  $R - \{n\pi \mid n \in \mathbb{Z}\}$                       (c)  $R - \{2n\pi \mid n \in \mathbb{Z}\}$                       (d)  $(-\infty, \infty)$

The domain of the function  $f(x) = {}^{16-x}C_{2x-1} + {}^{20-3x}P_{4x-5}$ , where the symbols have their usual meanings, is the set

[AMU 2002]

- (a)  $\{2, 3\}$                       (b)  $\{2, 3, 4\}$                       (c)  $\{1, 2, 3, 4\}$                       (d)  $\{1, 2, 3, 4, 5\}$

Domain of the function  $f(x) = \sin^{-1}\{1 + e^x\}^{-1}$  is

[AMU 1999]

- (a)  $(-\infty, \infty)$                       (b)  $[-1, 0]$                       (c)  $[0, 1]$                       (d)  $[-1, 1]$

If  $n$  is an integer then domain of the function  $\sqrt{\sin 2x}$  is

[MP PET 2003]

- (a)  $\left[n\pi - \frac{\pi}{2}, n\pi\right]$                       (b)  $\left[n\pi, n\pi + \frac{\pi}{2}\right]$                       (c)  $[(2n-1)\pi, 2n\pi]$                       (d)  $[2n\pi, (2n+1)\pi]$

## Range of Function

### Basic Level

If  $A = \{-2, -1, 0, 1, 2\}$  and  $f: A \rightarrow \mathbb{Z}, f(x) = x^2 + 1$ , then the range of  $f$  is

[Rajasthan PET 1995]

- (a)  $\{0, 1, 2, 5\}$                       (b)  $\{1, 2, 5\}$                       (c)  $\{-5, -2, 1, 2, 3\}$                       (d)  $A$

The range of the function  $f: [0, 1] \rightarrow \mathbb{R}, f(x) = x^3 - x^2 + 4x + 2 \sin^{-1} x$  is

- (a)  $[-\pi - 2, 0]$                       (b)  $[2, 3]$                       (c)  $[0, 4 + \pi]$                       (d)  $[0, 2 + \pi]$

The range of  $f(x) = \cos(x/3)$  is

[Rajasthan PET 2002]

- (a)  $[-1/3, 1/3]$                       (b)  $[-3, 3]$                       (c)  $[1/3, -1/3]$                       (d)  $[-1, 1]$

Range of  $f(x) = \frac{x^2 + 34x - 71}{x^2 + 2x - 7}$  is

[Roorkee 1983]

- (a)  $[5, 9]$                       (b)  $(-\infty, 5] \cup [9, \infty)$                       (c)  $(5, 9)$                       (d) None of these

Range of the function  $f(x) = \frac{x^2 - x + 1}{x^2 + x + 1}$

[Karnataka CET 1993]

- (a)  $\mathbb{R}$                       (b)  $[3, \infty)$                       (c)  $\left[\frac{1}{3}, 3\right]$                       (d) None of these

### Advance

The range of the function  $f(x) = \cos[x]$ , where  $\frac{-\pi}{2} < x < \frac{\pi}{2}$  is

[Karnataka CET 1994]

- (a)  $\{-1, 1, 0\}$                       (b)  $\{\cos 1, 1, \cos 2\}$                       (c)  $\{\cos 1, -\cos 1, 1\}$                       (d) None of these



The range of the function  $f(x) = |x-1| + |x-2|$ ,  $-1 \leq x \leq 3$  is

- (a) [1, 3] (b) [1, 5] (c) [3, 5] (d) None of these

Let  $f(x) = (1 + b^2)x^2 + 2bx + 1$  and  $m(b)$  the minimum value of  $f(x)$  for a given  $b$ . As  $b$  varies, the range of  $m(b)$  is

[IIT Screening 2001]

- (a) [0, 1] (b)  $\left[0, \frac{1}{2}\right]$  (c)  $\left[\frac{1}{2}, 1\right]$  (d) (0, 1]

## Kind of Functions

### Basic Level

Which of the following functions defined from  $R$  to  $R$  is onto

[Rajasthan PET 1985, 86]

- (a)  $f(x) = |x|$  (b)  $f(x) = e^{-x}$  (c)  $f(x) = x^3$  (d)  $f(x) = \sin x$

The number of bijective function from set  $A$  to itself when  $A$  contains 106 elements is

[EAMCET 1994]

- (a) 106 (b)  $(106)^2$  (c)  $106!$  (d)  $2^{106}$

If  $A$  contains 3 elements and  $B$  contains 4 elements, then the number of all one – one functions defined from  $A$  to  $B$  is

[EAMCET 1992; UPSEAT 2001]

- (a) 144 (b) 12 (c) 24 (d) 64

If  $A = \{a, b\}$ , then total number of functions which can be defined from  $A$  to  $A$  is

- (a) 2 (b) 3 (c) 4 (d) 1

Function  $f: R \rightarrow R, f(x) = x^3 + 7$  is

[Rajasthan PET 1984]

- (a) One – one onto (b) One – one into (c) Many – one onto (d) Many – one into

Which of the following functions from  $R$  to  $R$  is into

[Rajasthan PET 1984]

- (a)  $x^5$  (b)  $3x - 7$  (c)  $x^3$  (d)  $\sin x$

Function  $f: R \rightarrow R, f(x) = x^2$  is

[IIT 1970; MP PET 1997]

- (a) One – one but not onto (b) Onto but not one- one (c) Neither one-one nor onto (d) One- one onto

If  $A = R - \{3\}, B = R - \{1\}$  and  $f: A \rightarrow B, f(x) = \frac{x-2}{x-3}$ , then  $f$  is

- (a) One-one (b) Onto (c) One-one onto (d) Many-one into

### Advance

Let  $f(x) = \frac{x^2 - 4}{x^2 + 4}$  for  $|x| > 2$ , then the function  $f: (-\infty, -2] \cup [2, \infty) \rightarrow (-1, 1)$  is

[Orissa JEE 2002]

- (a) One-one into (b) One-one onto (c) Many one into (d) Many one onto

Let the function  $f: R \rightarrow R$  be defined by  $f(x) = 2x + \sin x, x \in R$ . Then  $f$  is

[IIT Screening 2002]

- (a) One-to-one and onto (b) One-to-one but not onto  
(c) Onto but not one-to-one (d) Neither one-to-one nor onto

function  $f: R \rightarrow R, f(x) = x|x|$  is

[Rajasthan PET 1991, 98]

- (a) One – one but not onto (b) Onto but not one – one  
(c) One – one onto (d) Neither one – one nor onto

If for two function  $f$  and  $g$ ;  $g \circ f$  is a bijection, then correct statement is

[Haryana CEE 1998]

- (a) Both  $g$  and  $f$  must be bijections (b)  $g$  must be a bijection



(c)  $f$  must be a bijection

(d) Neither of them may be a bijection

If  $f: [0, \infty) \rightarrow [0, \infty)$  and  $f(x) = \frac{x}{1+x}$ , then  $f$  is

[IIT Screening 2003]

(a) One - one and onto (b) One - one but not onto (c) Onto but not one - one (d) Neither one - one nor onto

The number of all onto functions which can be defined from  $A = \{1, 2, 3, \dots, n\}$ ,  $n \geq 2$  to  $B = \{a, b\}$  is

[IIT Screening 1992]

(a)  ${}^n P_2$  (b)  $2^n - 2$  (c)  $2^n - 1$  (d) None of these

If  $1 + 2x$  is a function having  $\left(\frac{-\pi}{2}, \frac{\pi}{2}\right)$  as domain and  $(-\infty, \infty)$  as co-domain, then it is

[IIT 1992]

(a) Onto but not one - one (b) One - one but not onto (c) One - one and onto (d) Neither one - one nor onto

If  $A = \{x \mid -1 \leq x \leq 1\} = B$  and  $f: A \rightarrow B$ ,  $f(x) = \sin \pi x$ , then  $f$  is

(a) One - one (b) Onto (c) One - one onto (d) Many one into

If the real-valued function  $f(x) = px + \sin x$  is a bijective function then the set of possible values of  $p \in R$  is

(a)  $R - \{0\}$  (b)  $R$  (c)  $(0, +\infty)$  (d) None of these

## Even/Odd Functions

### Basic Level

The function  $f(x) = x \cos x$  is

(a) Even function (b) Odd function (c) Neither even nor odd (d) Periodic function

A function whose graph is symmetrical about the  $y$ -axis is given by

(a)  $f(x) = \log_e(x + \sqrt{x^2 + 1})$  (b)  $f(x + y) = f(x) + f(y)$  for all  $x, y \in R$   
(c)  $f(x) = \cos x + \sin x$  (d) None of these

Let  $f(x + y) = f(x) + f(y)$  for all  $x, y \in R$ . Then

(a)  $f(x)$  is an even function (b)  $f(x)$  is an odd function (c)  $f(0) = 0$  (d)  $f(n) = nf(1), n \in N$

If  $f(x)$  is an odd function then

(a)  $\frac{f(-x) + f(x)}{2}$  is an even function (b)  $[|f(x)| + 1]$  is even, where  $[x]$  is the greatest integer  $\leq x$   
(c)  $\frac{f(x) - f(-x)}{2}$  is neither even nor odd (d) None of these

### Advance

If  $f(x)$  and  $g(x)$  are two functions of  $x$  such that  $f(x) + g(x) = e^x$  and  $f(x) - g(x) = e^{-x}$  then

(a)  $f(x)$  is an odd function (b)  $g(x)$  is an odd function (c)  $f(x)$  is an even function (d)  $g(x)$  is an even function

If  $f(x) = \begin{cases} x^2 \sin \frac{\pi x}{2}, & |x| < 1 \\ |x| |x|, & |x| \geq 1 \end{cases}$  then  $f(x)$  is

(a) An even function (b) An odd function (c) A periodic function (d) None of these

Which of the following is an even function? Here  $[.]$  denotes the greatest integer function and  $f$  is any function

(a)  $[x] - x$  (b)  $f(x) - f(-x)$  (c)  $e^{3-2x} \cdot \tan^2 x$  (d)  $f(x) + f(-x)$

## Periodic Function

### Basic Level



The period of  $|\cos x|$  is

[Rajasthan PET 1998]

- (a)  $2\pi$  (b)  $\pi$  (c)  $\frac{\pi}{2}$  (d)  $\frac{3\pi}{2}$

The period of the function  $\sin\left(\frac{\pi x}{2}\right) + \cos\left(\frac{\pi x}{2}\right)$  is

[EAMCET 1990]

- (a) 4 (b) 6 (c) 12 (d) 24

If  $f(x)$  is a periodic function of the period  $T$ , then  $f(ax + b)$  where  $a > 0$ , is a periodic function of the period

[AMU 2000]

- (a)  $T/b$  (b)  $aT$  (c)  $bT$  (d)  $T/a$

The period of the function  $f(x) = \sin\left(\frac{2x+3}{6\pi}\right)$  is

- (a)  $2\pi$  (b)  $6\pi$  (c)  $6\pi^2$  (d) None of these

The period of the function  $f(x) = 3 \sin \frac{\pi x}{3} + 4 \cos \frac{\pi x}{4}$  is

- (a) 6 (b) 24 (c) 8 (d)  $2\pi$

The period of the function  $f(x) = |\sin x| + |\cos x|$  is

- (a)  $\pi$  (b)  $\pi/2$  (c)  $2\pi$  (d) None of these

### Advance

Let  $f(x) = \cos 3x + \sin \sqrt{3}x$ . Then  $f(x)$  is

- (a) A periodic function of period  $2\pi$  (b) A periodic function of period  $\sqrt{3}\pi$   
(c) Not a periodic function (d) None of these

$f(x) = \cos \sqrt{x}$ , correct statement is

[Haryana CEE 1998]

- (a)  $f(x)$  is periodic & its period  $= \sqrt{2}\pi$  (b)  $f(x)$  is periodic & its period  $= 4\pi^2$   
(c)  $f(x)$  is periodic & its period  $= \sqrt{\pi}$  (d)  $f(x)$  is not periodic

### Composite Functions

#### Basic Level

If  $f: R \rightarrow R, f(x) = \sin x; g: R \rightarrow R, g(x) = x^2$ , then  $(f \circ g)(x)$  equals to

[UPSEAT 1987, 2000]

- (a)  $\sin x^2$  (b)  $\sin^2 x$  (c)  $\sin x + x^2$  (d)  $\sin \frac{x}{x^2}$

If  $f(x) = (a - x^n)^{1/n}$ , where  $a > 0$  and  $n$  is a positive integer, then  $f[f(x)] =$

[IIT 1983; UPSET 2001]

- (a)  $x^3$  (b)  $x^2$  (c)  $x$  (d) None of these

If  $f(x) = \frac{x}{\sqrt{1+x^2}}$ , then  $f \circ f \circ f(x)$  is equal to

[Rajasthan PET 2000]



- (a)  $\frac{x}{\sqrt{1+3x^2}}$                       (b)  $\frac{x}{\sqrt{1+2x^2}}$                       (c)  $\frac{x}{\sqrt{1+x^2}}$                       (d) None of these

Let  $f$  and  $g$  be functions defined by  $f(x) = \frac{x}{x+1}$ ,  $g(x) = \frac{x}{1-x}$ , then  $(f \circ g)(x)$  is

- (a)  $\frac{1}{x}$                       (b)  $\frac{1}{x-1}$                       (c)  $x-1$                       (d)  $x$

If  $f(x) = ax + b$  and  $g(x) = cx + d$ , then  $f(g(x)) = g(f(x))$  is equivalent to

[UPSEAT 2001]

- (a)  $f(a) = g(c)$                       (b)  $f(b) = g(b)$                       (c)  $f(d) = g(b)$                       (d)  $f(c) = g(a)$

### Advance

If  $f(x) = \sqrt{|x-1|}$  and  $g(x) = \sin x$ , then  $(f \circ g)(x)$  is equal to

[Roorkee 1992]

- (a)  $\sin \sqrt{|x-1|}$                       (b)  $|\sin x/2 - \cos x/2|$                       (c)  $|\sin x - \cos x|$                       (d) None of these

If  $f$  and  $g$  are two real valued function defined by  $f(x) = e^x$  and  $g(x) = 3x - 2$ , then  $(f \circ g)^{-1}(x)$  is equal to

[Roorkee 1998]

- (a)  $\log(3x - 2)$                       (b)  $\frac{2 + \log x}{3}$                       (c)  $\log\left(\frac{x+2}{3}\right)$                       (d) None of these

If  $f(x) = \frac{1}{1-x}$ ,  $x \neq 0, 1$ , then the graph of the function  $y = f\{f(f(x))\}$ ,  $x > 1$ , is

- (a) A circle                      (b) An ellipse                      (c) A straight line                      (d) A pair of straight lines

If  $f(x)$  is defined on  $[0, 1]$  by the rule  $f(x) = \begin{cases} x, & \text{if } x \text{ is rational} \\ 1-x, & \text{if } x \text{ is irrational} \end{cases}$ . Then for all  $x \in [0, 1]$ ,  $f(f(x))$  is

- (a) Constant                      (b)  $1+x$                       (c)  $x$                       (d) None of these

## Inverse Function

### Basic Level

$f: R \rightarrow R$  is a function defined by  $f(x) = 10x - 7$ . If  $g = f^{-1}$ , then  $g(x) =$

[EAMCET 1993]

- (a)  $\frac{1}{10x-7}$                       (b)  $\frac{1}{10x+7}$                       (c)  $\frac{x+7}{10}$                       (d)  $\frac{x-7}{10}$

If  $y = f(x) = \frac{x+2}{x-1}$ , then  $x =$

[IIT 1984]

- (a)  $f(y)$                       (b)  $2f(y)$                       (c)  $\frac{1}{f(y)}$                       (d) None of these

Inverse of the function  $y = 2x - 3$  is

[UPSEAT 2002]

- (a)  $\frac{x+3}{2}$                       (b)  $\frac{x-3}{2}$                       (c)  $\frac{1}{2x-3}$                       (d) None of these

### Advance

The value of  $\alpha$  for which the function  $f(x) = 1 + \alpha x$ ,  $\alpha \neq 0$  is inverse of itself will be

[IIT 1992]

- (a)  $-2$                       (b)  $-1$                       (c)  $1$                       (d)  $2$

If  $f: [1, +\infty) \rightarrow [2, +\infty)$  is given by  $f(x) = x + \frac{1}{x}$  then  $f^{-1}$  equals

[IIT Screening 2001]

- (a)  $\frac{x + \sqrt{x^2 - 4}}{2}$                       (b)  $\frac{x}{1+x^2}$                       (c)  $\frac{x - \sqrt{x^2 - 4}}{2}$                       (d)  $1 + \sqrt{x^2 - 4}$





The inverse of the function  $f(x) = \frac{10^x - 10^{-x}}{10^x + 10^{-x}}$  is

[Rajasthan PET 2001]

- (a)  $\log_{10}(2-x)$       (b)  $\frac{1}{2} \log_{10}\left(\frac{1+x}{1-x}\right)$       (c)  $\frac{1}{2} \log_{10}(2x-1)$       (d)  $\frac{1}{4} \log\left(\frac{2x}{2-x}\right)$

The inverse of the function  $f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} + 2$  is given by

[Haryana CEE 1996]

- (a)  $\log_e\left(\frac{x-2}{x-1}\right)^{\frac{1}{2}}$       (b)  $\log_e\left(\frac{x-1}{3-x}\right)^{\frac{1}{2}}$       (c)  $\log_e\left(\frac{x}{2-x}\right)^{\frac{1}{2}}$       (d)  $\log_e\left(\frac{x-1}{x+1}\right)^{-2}$

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# Answer Sheet

## Assignment (Basic & Advance Level)

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
c	a	a	c	a	b	c	b	b	d	b	c	d	a	d	c	b	c	b	d
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
a	b	d	d	c	b	c	c	c	b	b	b	b	c	b	a	d	c	b	a
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
a	b	b	c	d	b	c	b	b	d	c	c	c	c	a	d	c	c	c	a
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
c	a	b	b	b	b	d	b	d	b,c,d	a,b	b,c	b	d	b	a	d	c	b	b
81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98		
c	d	a	c	a	d	c	b	b	c	c	c	a	a	b	a	b	b		